

$$E_k = \frac{1}{2} m v^2 \quad E_p = \frac{1}{2} m \omega^2 x^2$$

$$E_T = E_k + E_p \quad v = \omega r.$$

$$E_k = \frac{1}{2} m \omega^2 (x_0^2 - x^2) \quad v = \omega \sqrt{x_0^2 - x^2}$$

$$E_T = \frac{1}{2} m \omega^2 x_0^2$$

Find the total energy of a pendulum that has a frequency of 24 Hz with an amplitude of 0.80 m and a mass of 16 kg.

$$E = \frac{1}{2} m \omega^2 x_0^2$$

$$\omega = 2\pi(24)$$

$$\omega = 48\pi$$

$$\omega = 2\pi f$$

$$E_T = \frac{1}{2}(16\text{kg})(48\pi)^2(0.80)$$

$$E_T = 116,426$$

$$\approx 120,000 \text{ J}$$

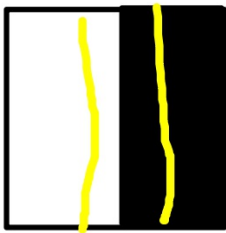
Find the total energy of a pendulum that has a period of 4.5 s with an amplitude of 0.75 m and a mass of 25 kg.

$$T = \frac{1}{f}$$

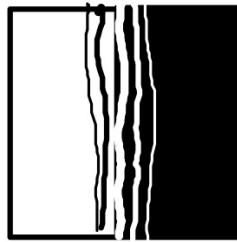
$$E_T = \frac{1}{2} m \omega^2 x_0^2$$

$$\omega = \frac{2\pi}{T}$$

Find the total energy of a pendulum that has a period of 0.45 s with an amplitude of 0.50 m and a mass of 33 kg.

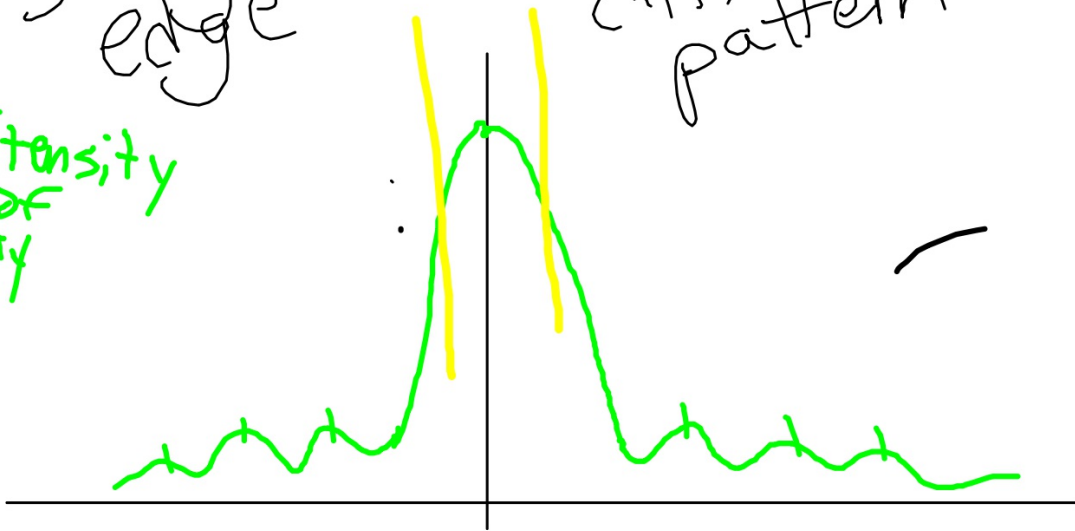


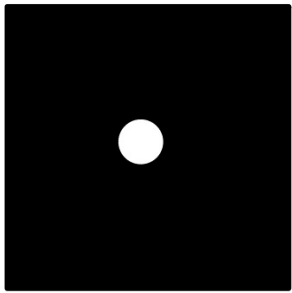
straight
edge



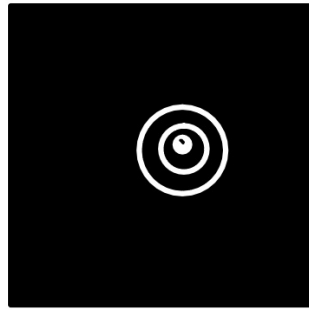
diff.
pattern

Intensity
of
ray

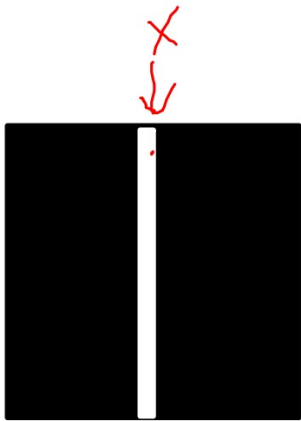




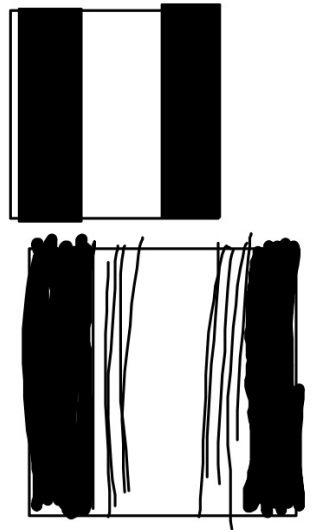
circular
aperture



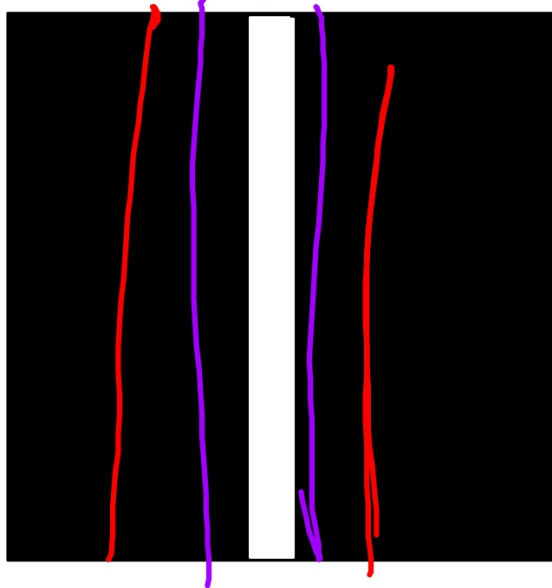
diffraction
pattern



Single
long
slit

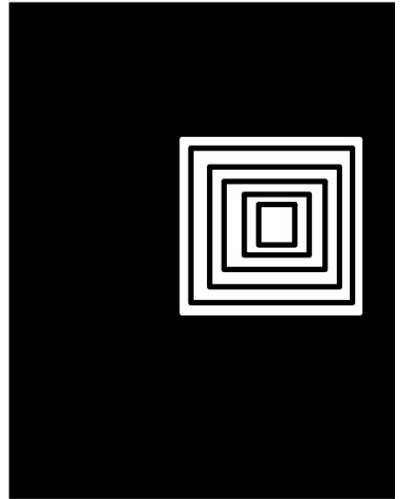
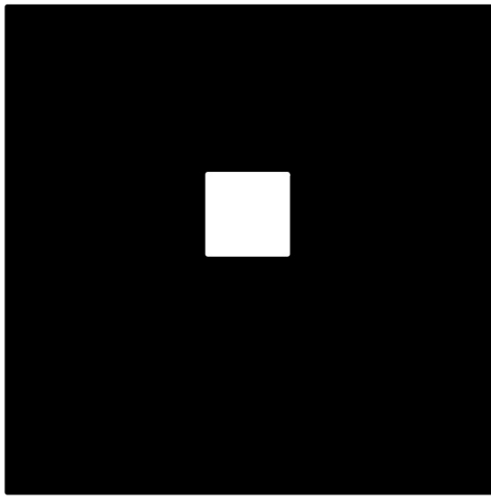


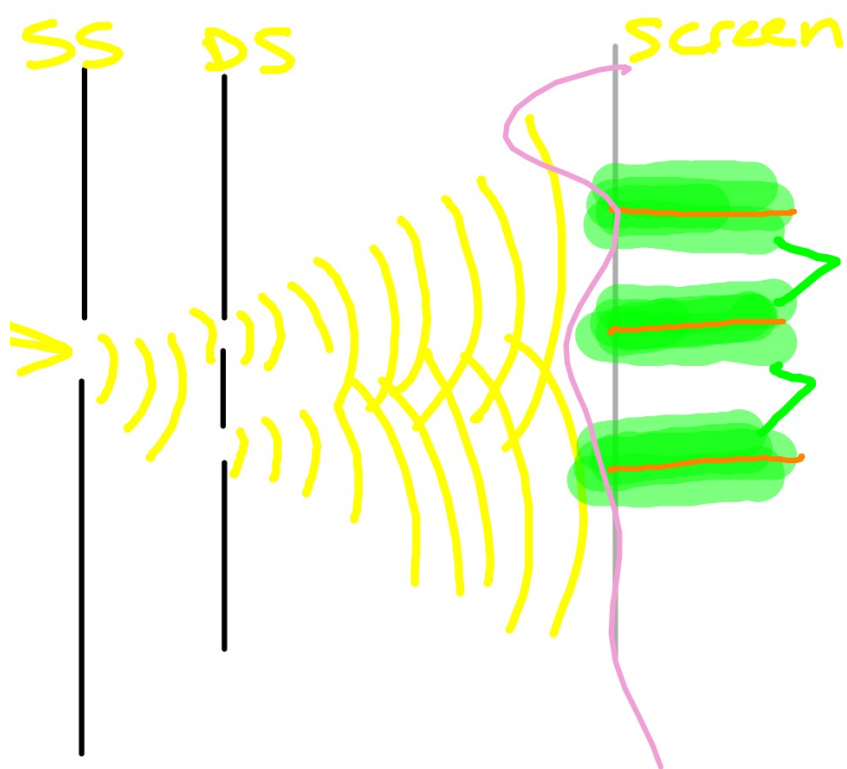
↓ white



roygbiv

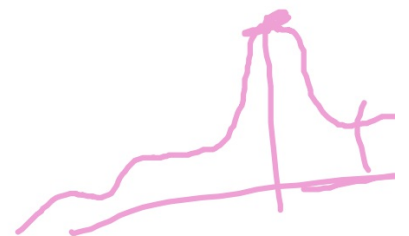


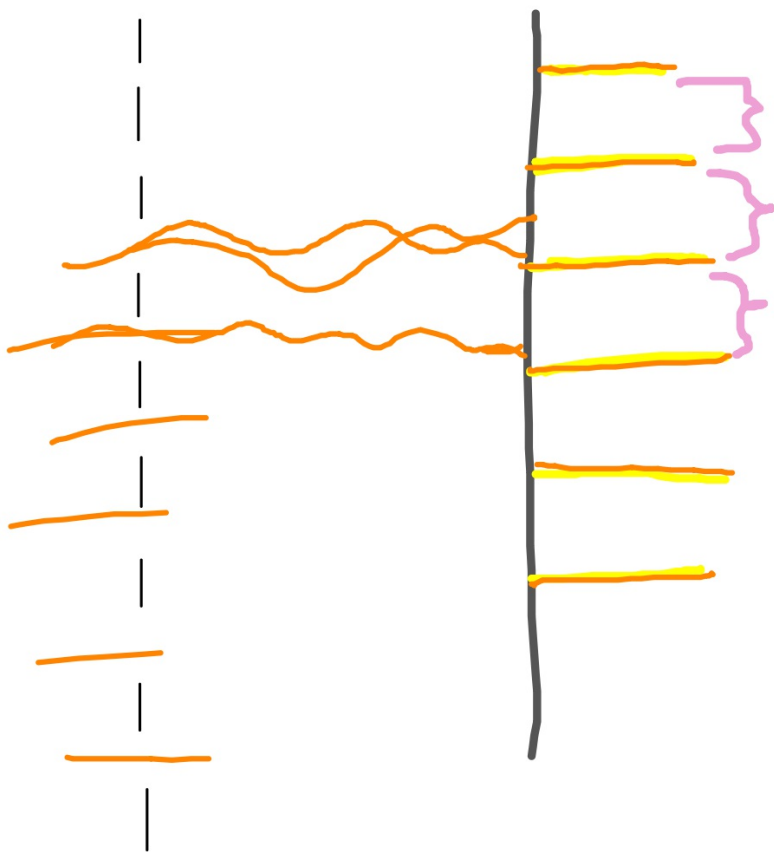




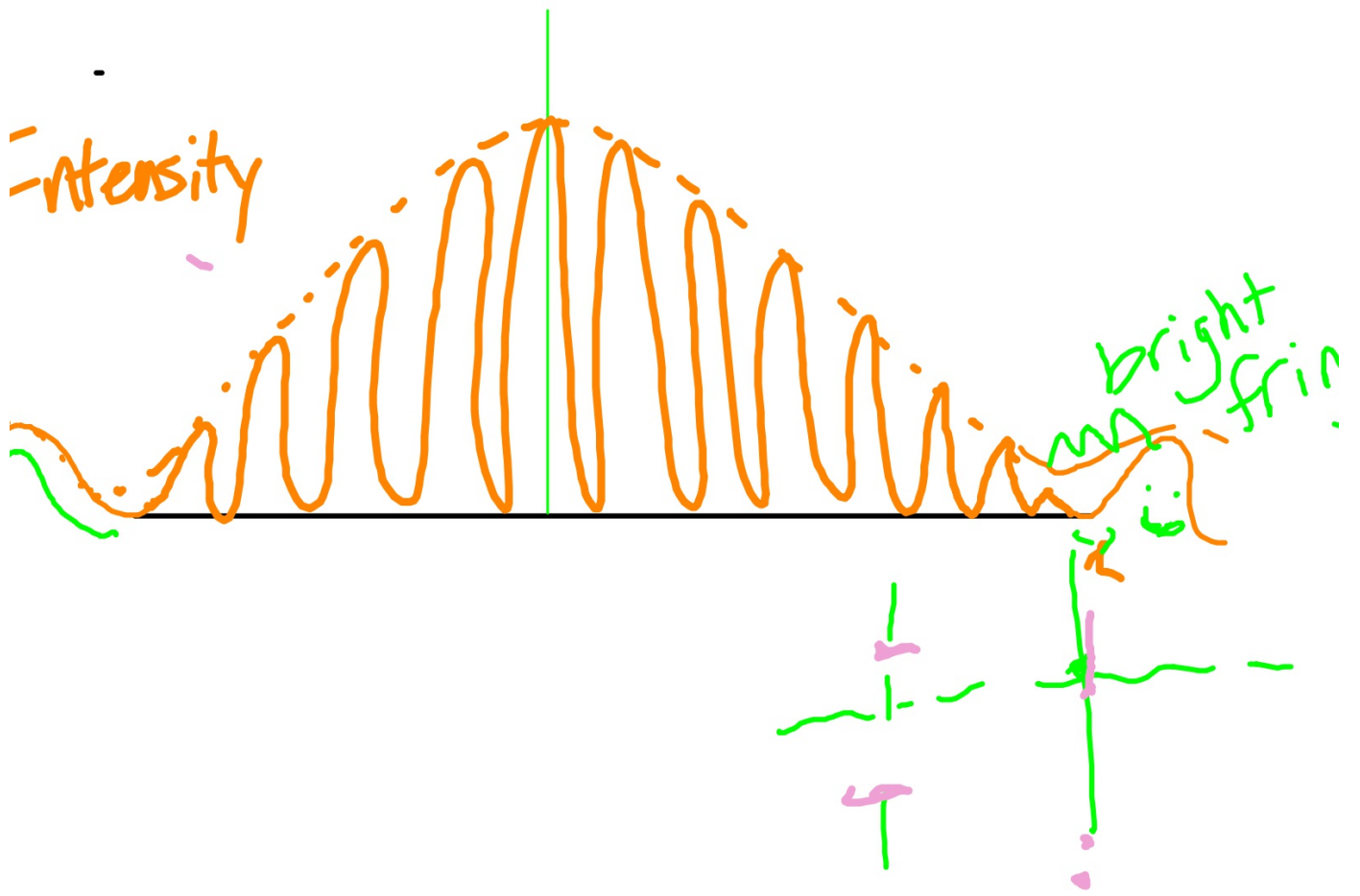
Diffraction
gradient

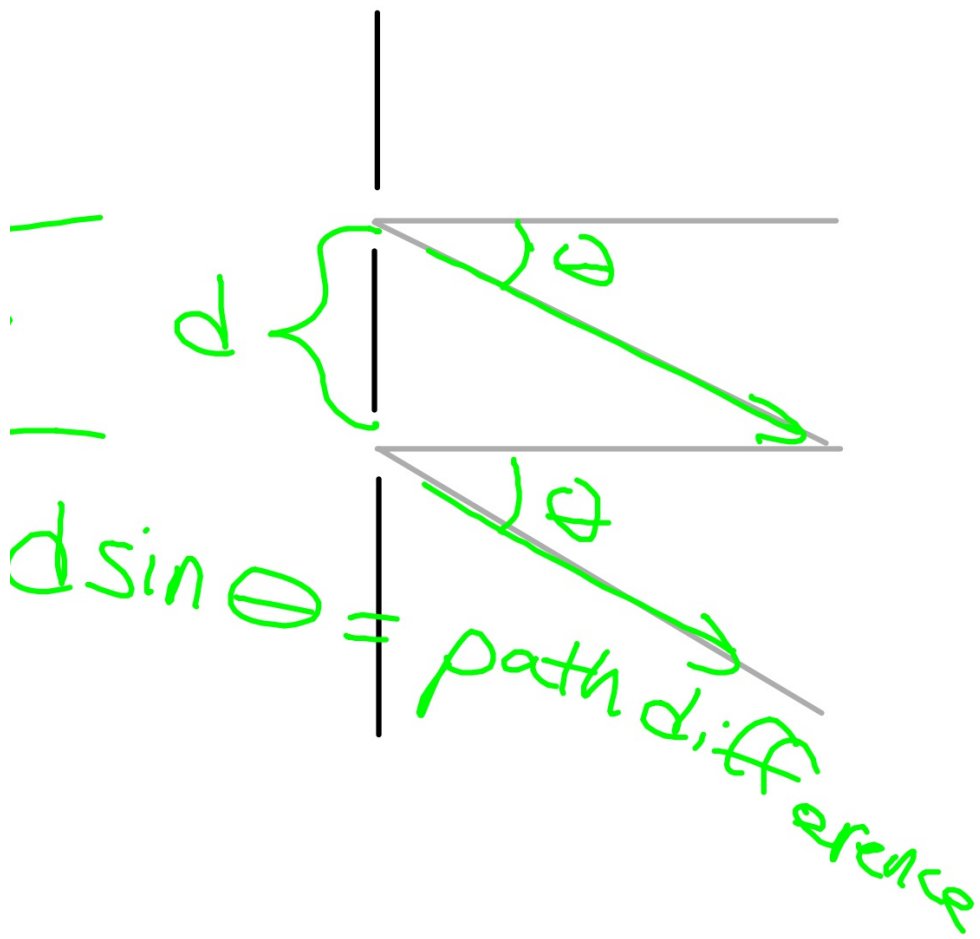
principal maxima





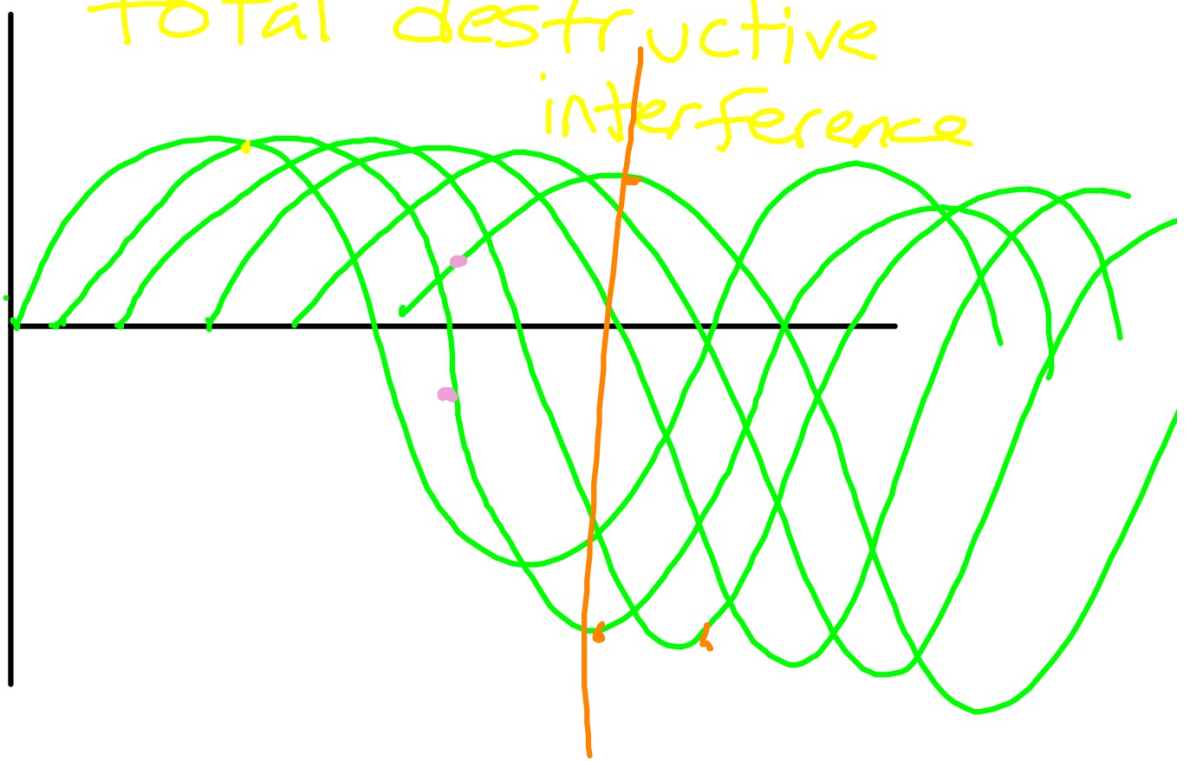
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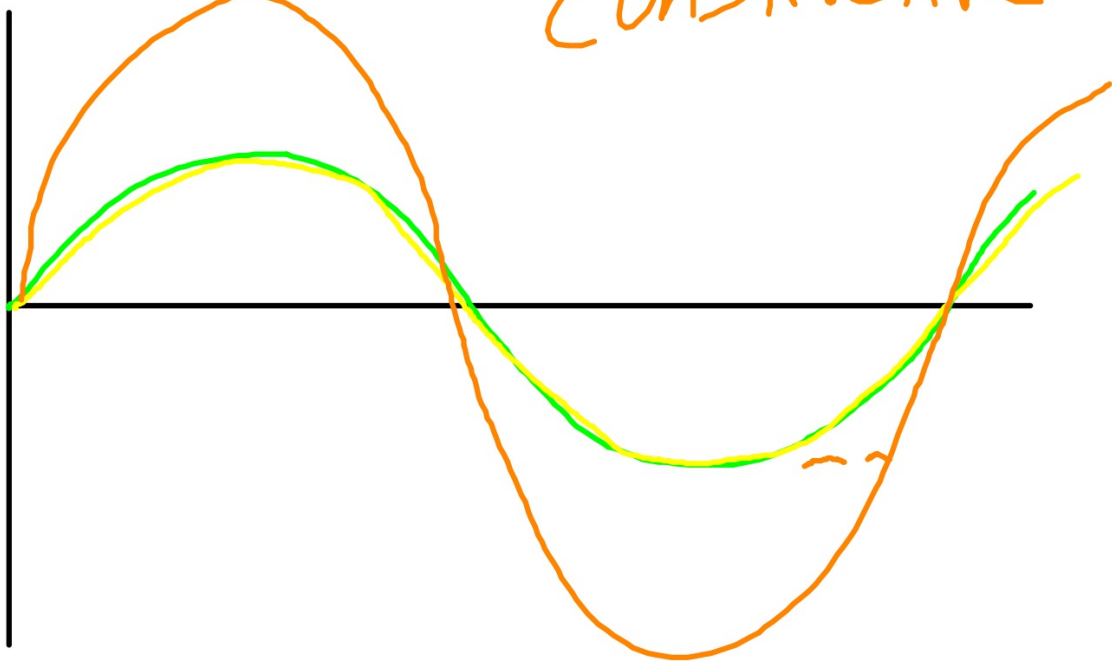


$$d \sin \theta = \text{path difference}$$

total destructive interference



constructive



Thin-film Interference



destructive interference

$$2tn = m\lambda$$

$n =$ refractive index

constructive interference

$$2tn = (m + \frac{1}{2})\lambda$$

Resolution



Slit $\Theta = \frac{\lambda}{b}$

Θ → min Θ for resolution

b → width of slit

Circular aperture $\Theta = \frac{1.22 \lambda}{b}$

If the wavelength of a light beam is 500 nm and the sources of light are 1.8 m away. If a student has pupils with a diameter of 4 mm , how far away would a car have to be to distinguish the two headlights.

$$\theta = \frac{1.22 \lambda}{b} = \frac{(1.22)(500 \times 10^{-9} \text{ m})}{4 \times 10^{-3} \text{ m}} = 1.525 \times 10^{-4}$$

$$3 \times$$

$$\theta = \frac{x}{D}$$

$$\frac{x}{\theta} = D$$

$$\frac{1.8}{1.525 \times 10^{-4}} = 11800$$

10 km

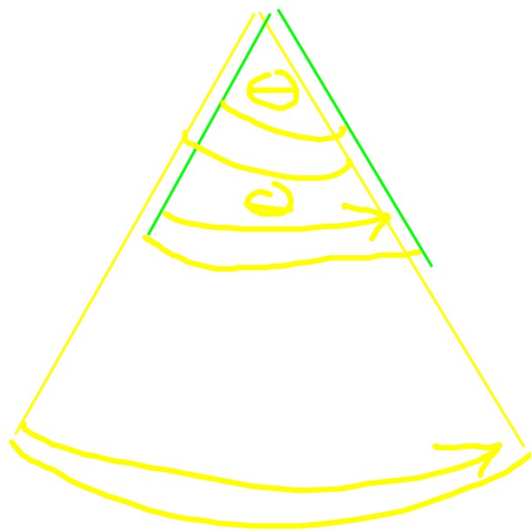
A student observes two distant sources of light. The wavelength of each source is 550 nm. The angular separation between these two sources is 2.5×10^{-4} radians subtended at the pupil of a student's eye.

Estimate the diameter of the pupil of the eye if the two images are just to be resolved.

A car drives by a standing person at a rate of 33 m/s. The person is screaming with a frequency of 1.8 kHz. After the car passes the person, what is the frequency of the sound if sound travels at 330 m/s?

$$f' = f \left(\frac{v' - v_o}{v} \right) = 1.8 \left(\frac{330 - 33}{330} \right) = 1.62 \text{ KHZ}$$

Two simple pendulum systems have the same mass, utilize the same small angle, but have different lengths of the bob. System 1 has a length of 1.8 m, while system 2 has a length of 4.2 m. Which has a longer period?



Doppler Effect w/ Light

$$= \lambda \frac{v}{c} \quad f' = f \left(\frac{v \pm v_0}{v} \right) \quad c = \underline{3.0 \times 10^8}$$

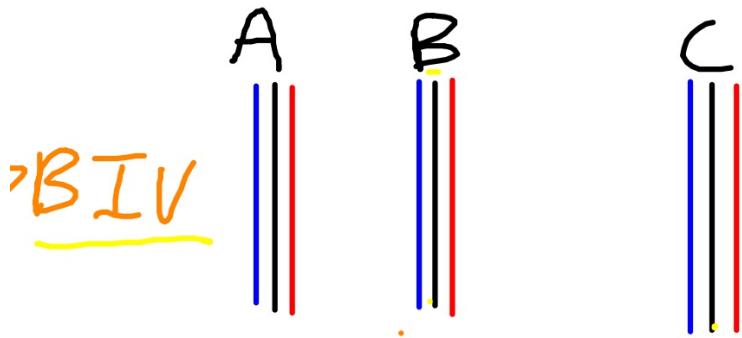
$f \lambda$

$$f' = f \left(\frac{v}{v \pm v_0} \right) \Rightarrow f' = f \left(1 \pm \frac{v_0}{v} \right)$$
$$f' = f \left(1 - \frac{v_0}{v} \right) \quad f' = f - f \frac{v_0}{v} \Rightarrow \Delta f =$$

As the Sun rotates, light waves received on Earth from opposite ends of a diameter show equal but opposite Doppler shifts. The speed of the edge of the Sun relative to the Earth is 1.90 km/s. What wavelength shift should be expected in the helium line having wavelength 587.5618 nm?

$$\Delta\lambda = \lambda \frac{v}{c} \quad \Delta\lambda = 0.0037 \text{ nm}$$

$$\Delta\lambda = 587.5618 \text{ nm} \left(\frac{1.90 \times 10^3 \text{ m/s}}{3.0 \times 10^8 \text{ m/s}} \right)$$



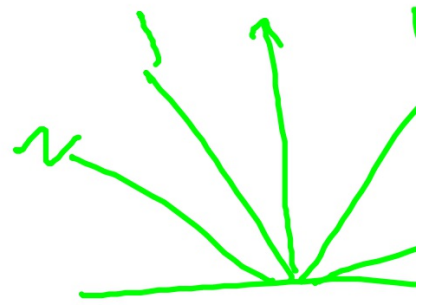
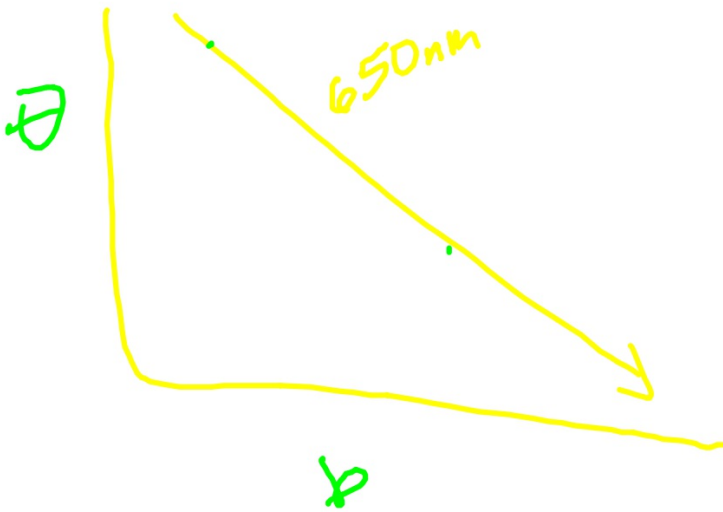
$$c = f\lambda$$



62.

$$\theta = \frac{\lambda}{b}$$

$$b\theta = \lambda$$



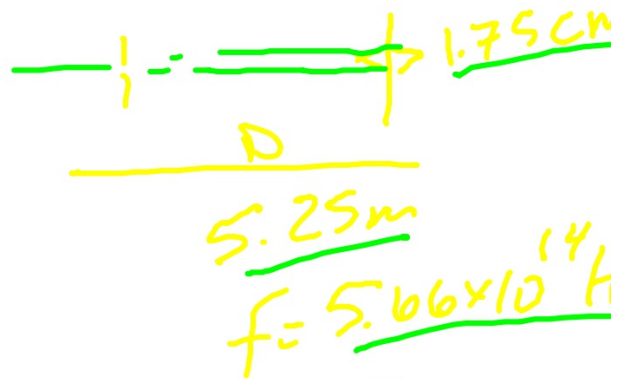
sol.

$$b = \frac{\lambda}{\theta}$$

$$\theta = \frac{x}{D}$$

$$\theta = \frac{\lambda}{b}$$

$$\therefore b = \frac{\lambda}{\theta} = \frac{D\lambda}{x}$$



$$c = f\lambda$$

$$\frac{Dc}{fx} = \lambda$$

$$\omega = \frac{2\pi}{T}$$

$$a = -\omega^2 x$$

$$x = x_0 \sin(\omega t)$$

$$v = \omega x_0 \cos(\omega t)$$

$$v = \pm \omega \sqrt{x_0^2 - x^2}$$

$$E_k = \frac{1}{2} m \omega^2 (x_0^2 - x^2)$$

$$E_T = \frac{1}{2} m \omega^2 x_0^2$$

$$T_{\text{per}} = 2\pi \sqrt{\frac{l}{g}}$$

$$T_s = 2\pi \sqrt{\frac{m}{k}}$$

$$\theta_{\text{slit}} = \frac{\lambda}{b} \quad \text{--- width}$$

$$\theta = \frac{x}{D} \quad \text{--- separation}$$

$$\theta = \frac{1.22 \lambda}{b}$$

$$n\lambda = d \sin \theta$$

distance between slits

$n = \text{integer}$

$$C_{\text{constructive}} \quad 2dn = (m + \frac{1}{2})\lambda$$

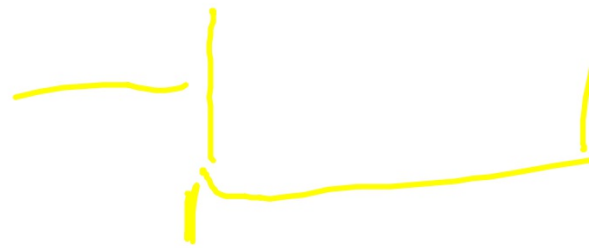
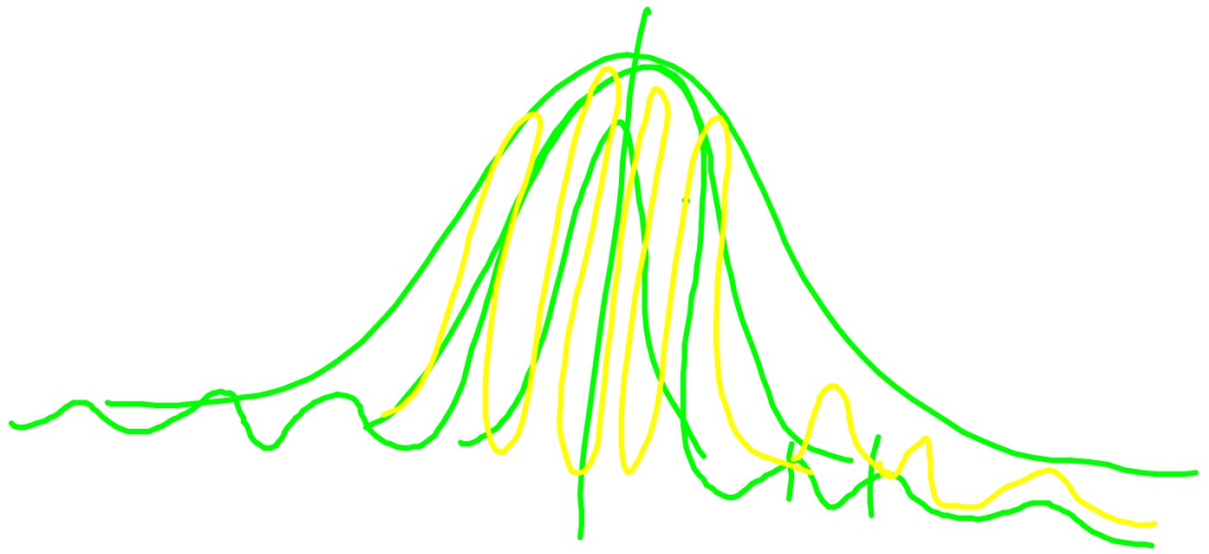
$$D_{\text{destructive}} \quad 2dn = m\lambda$$

$n = \text{refractive}$
 $m = \text{integer}$

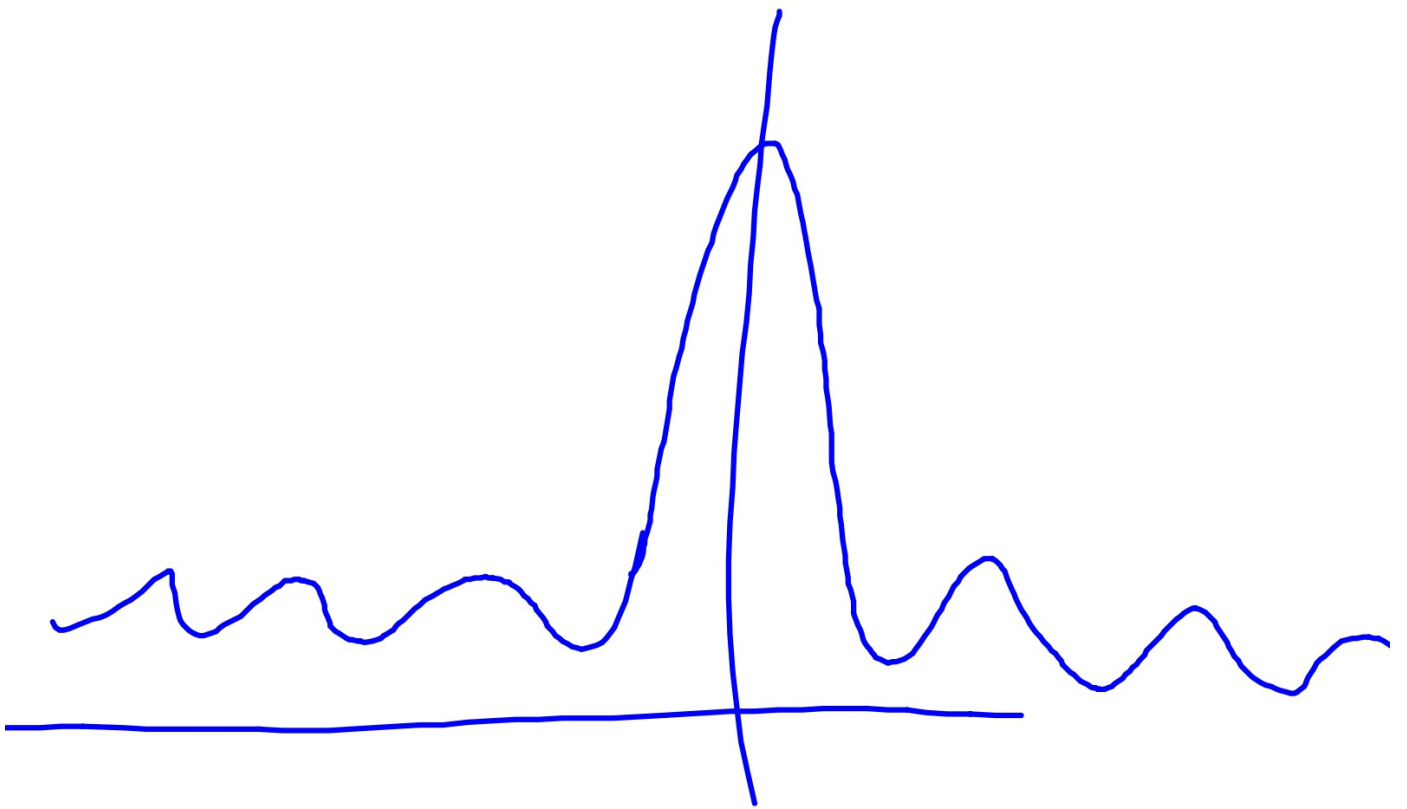
$$f' = f \left(\frac{v}{v \pm v_s} \right)$$

$$f' = f \left(\frac{v \pm v_o}{v} \right)$$

$$\Delta f = f \frac{v}{c} \quad \Delta \lambda = \lambda \frac{v}{c}$$







$$v = 345 \frac{m}{s} \quad f' = f \left(\frac{v \pm v_o}{v \pm v_s} \right)$$

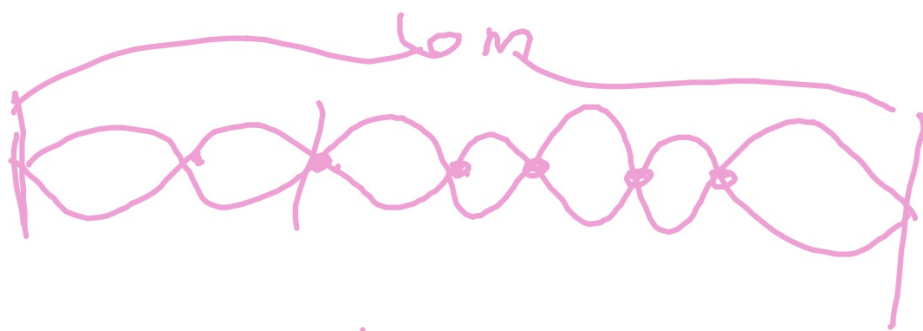
$$f = 512 \text{ Hz}$$

$$f' = 400 \text{ Hz}$$

$$v_o = 26.8 \frac{m}{s}$$

$$f' = f \left(\frac{v}{v \pm v_s} \right)$$





$$\frac{6}{7} \cdot 2 = \frac{12}{7} \text{ m}$$

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$$f' = f \left(\frac{V \pm V_{01s}}{V \mp V_{Sou}} \right)$$

